



Final EXAM 2014/2015- Second Term

Course	Electrical Circuits (2) (EPM1203)	Time Allowed	3 hours
Students	1 st Year (Electrical)	Total Marks	85
Date	Wed, June 10, 2015	Number of pages	3

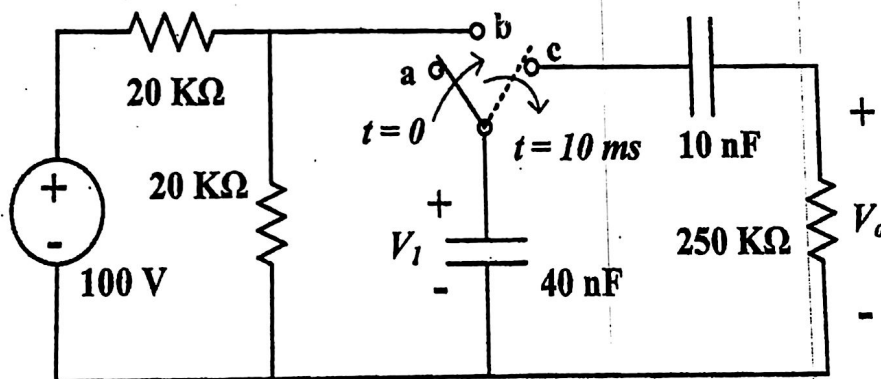
١. تجنب قدر المستطاع استخدام القلم الرصاص فيما سوى الرسومات.	تعليمات عامة
٢. اكتب رقم السؤال بوضوح.	
٣. تجنب تماما استخدام اللونين الأحمر والأخضر في إجاباتك.	
٤. لا تستخدم سائل التصحيح corrector	
٥. يراعى قدر المستطاع أن تبدأ إجابة كل سؤال في صفحة جديدة.	
٦. لا يشترط الإجابة بترتيب الأسئلة في ورقة الامتحان.	
٧. أجب بوضوح سواء باللغة الإنجليزية أو العربية.	

Answer ALL the following FIVE questions and problems:

- Clarify your answer with the suitable sketches of complete data as you can.
- Assume any missed data reasonably.

The first question (12 marks)

The switch in the circuit shown in figure has been in position "a" for a long time while initial charge on both capacitors was zero. At $t = 0$, the switch has been moved to position "b". After a time of 10 ms, it has been moved to position "c". Find and plot time expressions for v_o and v_i



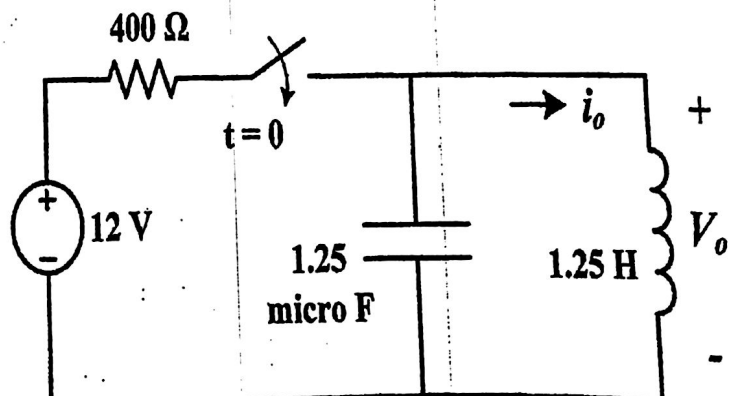
The second question (16 marks)

- With suitable relations and illustrations compare between the effect of resistance R on the step-response of parallel and series RLC circuits. (4 marks)

- In the circuit in figure, there was no stored energy when the switch is closed at time $t=0$.

Find time expressions of both v_o and i_o for $t \geq 0$

(12 marks)



PLEASE TURN OVER

The third question (20 marks)

a) The magnitude of the phase voltage of an ideal balanced three-phase Y-connected (four-wire) source is 240 V. The source is connected to a balanced Y-connected load by a distribution line that has impedance of $0.4 + j1.5 \Omega/\text{phase}$. The per-phase impedance of the load is $21.6 + j4.5 \Omega$. The phase sequence of the source is acb. Use the a-phase voltage of the source as the reference. (9 Marks)

(i) Construct a single-phase equivalent circuit. 1

$$Z = 22.8 \angle 15.26^\circ$$

(ii) Specify the magnitude and phase angle of the following:

1. The four line-currents 2

$$I_{LA} = 10.53 \angle -15.26^\circ$$

2. The three line-voltages at the terminals of the source 2

$$V_{L1} = 415 \angle -30^\circ$$

3. The three line-voltages at the terminals of the load 2

$$V_{L2} = 402.41 \angle 33.49^\circ$$

(iii) Calculate the total instantaneous power delivered by the generator. 2

$$P = 7314.28$$

b) Two balanced Δ -connected loads, with impedances $20 \angle -60^\circ \Omega$ and $18 \angle 45^\circ \Omega$, respectively, are connected to a three-phase system for which a line voltage is $V_{BC} = 212 \angle 0^\circ$ V. (11 Marks)

(i) Obtain the per-phase average, reactive and complex power of each load. 4

$$P = 23.66$$

(ii) Specify the magnitude and phase-angle of the three line currents I_{aA} , I_{bB} and I_{cC} . 4

$$I_{aA} = 23.66$$

(iii) Compute the total delivered power, and compare with the sum of the phases power 2

$$P = 28668.3$$

The fourth question (18 marks)

a) Two magnetically-coupled coils have self-inductances $L_1 = 50$ mH and $L_2 = 200$ mH, and a coefficient of coupling $k = 0.5$. If coil 2 has 1000 turns, and $i_1 = 5.0 \sin 400t$ (A), (5 Marks)

(i) Find the induced voltage at coil 2 and the flux of coil 1, Φ_1 . 3

$$100 \cos 400t \text{ V}$$

(ii) Determine the number of turns of the first coil. (Assume that the physical structure of these coupled coils is such that the P_{11} and P_{22} are equal). 1

$$500 \text{ turns}$$

(iii) What is the value of P_1 and P_2 ? 1

$$0.2 \times 10^6$$

b) The circuit shown has two magnetically-coupled coils with a maximum coefficient of coupling. (10 Marks)

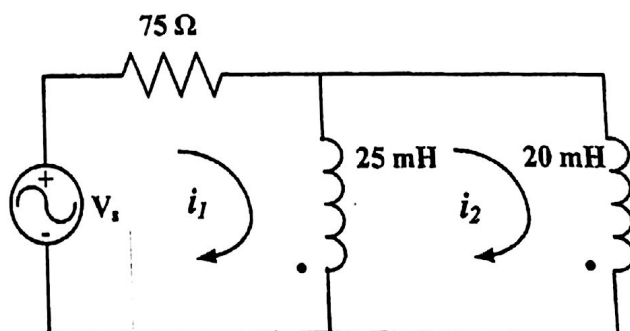
(i) Determine the mutual inductance between the two magnetically-coupled coils. 2

$$22.36 \text{ mH}$$

(ii) Write a set of mesh-current equations that describe the circuit in terms of i_1 and i_2 (in both time and frequency domain). 4

(iii) Simplify the parallel branches, containing 25 mH and 20 mH coils, to a single equivalent coil. 2

(iv) Starting with the stored energy calculation form, derive an expression of the maximum mutual inductance between two magnetically-coupled coils. 3



c) Show how the polarity marking on the two magnetically-coupled coils can be determined experimentally. (3 Marks)

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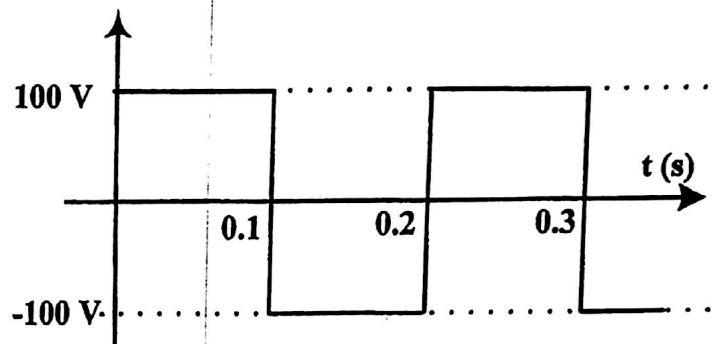
The fifth question (20 marks)

1. Sketch with sufficient details the input-output characteristics of operational amplifier. (3 marks)

2. With the aid of a circuit diagram and suitable relations, explain how an operational amplifier can be used to get difference between two signals. Clarify how to achieve unity scaling factors. (4 marks)

3. The shown voltage waveform represents the input to an integrating amplifier. The positive power supply terminal is connected to +15 V, while the negative terminal is connected to -10 V. Sketch the output voltage waveform.

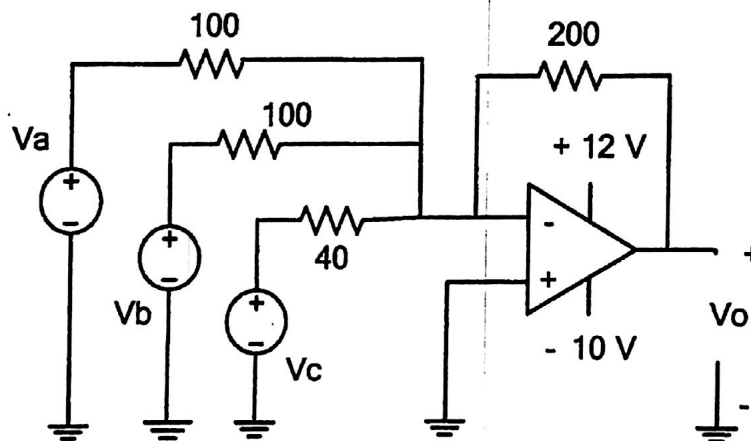
(4 marks)



4. The operational amplifier shown in figure is ideal. The values of the shown resistances are in $k\Omega$. Specify the range of V_c required to avoid amplifier saturation when

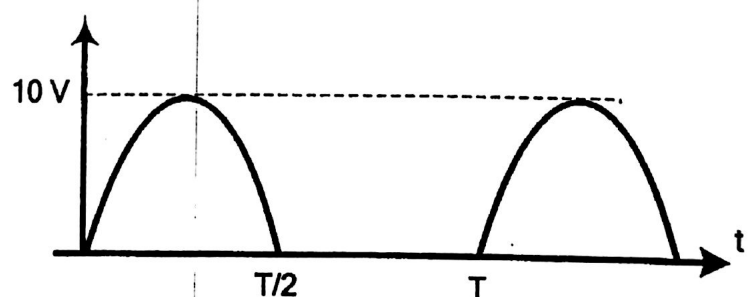
$$V_a = 3\text{ V} \quad \text{and} \quad V_b = 2\text{ V}$$

(4 marks)



5. Find the Fourier series spectrum of the half-wave rectified sinusoidal voltage shown in figure

(5 marks)



Good Luck and best wishes

Prof. Essam Eddin M. Rashad, Dr. Said M. Allam and exam committee

The Second Question

CIT 17113

①

Parallel

$$\frac{d^2 v}{dt^2} + \left(\frac{1}{RC}\right) \frac{dv}{dt} + \left(\frac{1}{LC}\right) v = 0$$

2nd order

$$\alpha = \frac{1}{2RC}$$

Series

$$\frac{d^2 i}{dt^2} + \left(\frac{R}{L}\right) \frac{di}{dt} + \left(\frac{1}{LC}\right) i = 0$$

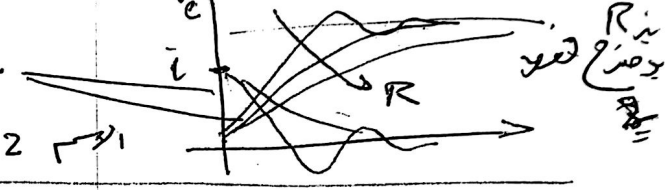
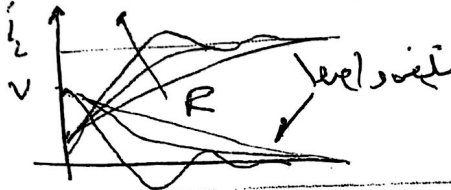
$\alpha = \frac{R}{2L}$

$$\alpha = \frac{R}{2L}$$

$\alpha > \omega_0$

over

$$\alpha = \frac{1}{2RC}$$



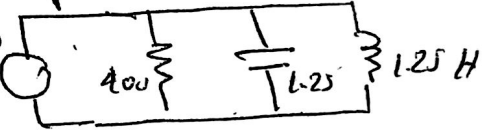
②

$$\alpha = \frac{1}{2RC} = 1000$$

$$\omega_0 = \frac{1}{\sqrt{LC}} = 800$$

overdamped

30 mA



$$s_1 = -400 \quad s_2 = -1600$$

$$V_o = V_f + A_1 e^{-400t} + A_2 e^{-1600t}$$

$$V_f = 0$$

$$V_o(0) = 0$$

$$A_1 + A_2 = 0$$

$$i'(0) = 30 \text{ mA}$$

$$\frac{di(0)}{dt} = \frac{dV_o(0)}{dt} = 24000$$

$$-400A_1 + 1600A_2 = 24000$$

By

$$A_1 = 20 \quad A_2 = -20$$

$$V_o = 20 e^{-400t} - 20 e^{-1600t}$$

$$i_o = I_f + A_1' e^{-400t} + A_2' e^{-1600t}$$

$$I_f = 30 \text{ mA}$$

$$i_o(0) = 0$$

$$0 = 30 + A_1' + A_2'$$

$$A_1' = -40 \text{ mA}$$

$$A_2' = 10 \text{ mA}$$

$$i_o' = 30 - 40 e^{-400t} + 10 e^{-1600t}$$

$$L \frac{di_o}{dt} \rightarrow V_o$$

check or another value

نموذج اطباء (سأله در انالیز)

مقدارهای

محاسبه

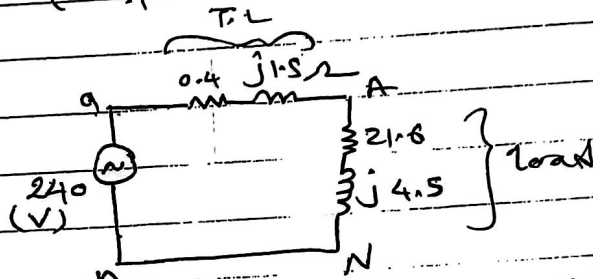
Q.9: [a]

$$I_{aA} = \frac{V_{an}}{Z_{TL} + Z_L}$$

$$= \frac{240 \angle 0^\circ}{22 + j6}$$

$$= \frac{240 \angle 0^\circ}{22.8 \angle 15.26^\circ}$$

$$= 10.53 \angle -15.26^\circ \text{ A}$$



single Eq. circuit (i)

$$I_{bB} = 10.53 \angle 104.74^\circ \text{ A}$$

$$I_{cC} = 10.53 \angle -135.26^\circ \text{ A}$$

$$I_{nN} = \text{Zero}$$

$$V_{ab} = \sqrt{3} \angle 30^\circ V_{an}$$

$$= 415 \angle -30^\circ \text{ V}$$

$$V_{bc} = 415 \angle 90^\circ \text{ V}$$

$$V_{ca} = 415 \angle -150^\circ \text{ V}$$

the line voltage at
(2) the source terminals

$$V_{AN} = I_{aA} Z_L = 10.53 \angle -15.26^\circ \times 22.064 \angle 11.77^\circ$$

$$= 232.33 \angle -3.49^\circ \text{ volt}$$

$$V_{AB} = \sqrt{3} \angle 30^\circ V_{AN} = 402.41 \angle -33.49^\circ \text{ volt}$$

$$V_{BC} = 402.41 \angle 86.51^\circ \text{ volt}$$

$$V_{CA} = 402.41 \angle -153.49^\circ \text{ volt}$$

line
voltage
at the load
terminals

$$(iii) P = 3 V_{ph} I_{ph} \cos \phi$$

$$= 3 \times 240 \times 10.53 \cos(15.26^\circ)$$

$$= 7314.28 \text{ watt}$$

The Second Question

CIR 2 17/11

①

Parallel

$$\frac{d^2 v}{dt^2} + \left(\frac{1}{RC}\right) \frac{dv}{dt} + \left(\frac{1}{LC}\right) v = 0$$

2nd order

series

$$\frac{di}{dt} + \frac{R}{L} \frac{di}{dt} + \frac{1}{LC} i = 0$$

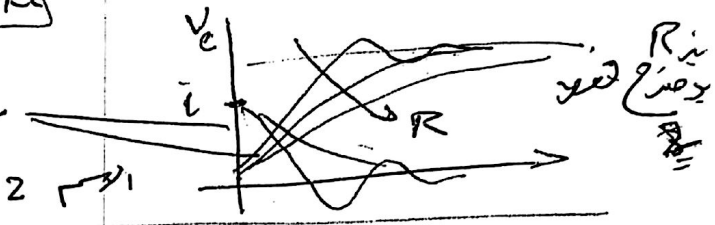
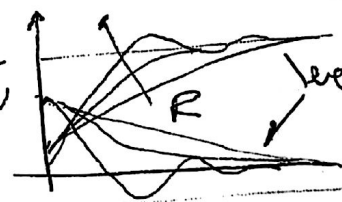
$$\alpha = \frac{R}{2L}$$

④

$\alpha > \omega_0$

over

$$\alpha = \frac{1}{2RC}$$



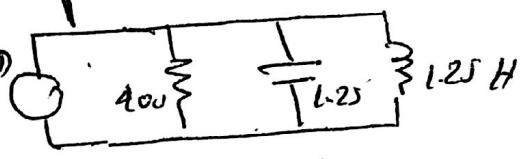
②

$$\alpha = \frac{1}{2RC} = 1000$$

$$\omega_0 = \frac{1}{\sqrt{LC}} = 800$$

over damped

30 mA



$$s_1 = -400 \quad s_2 = -1600$$

$$V_o = V_f + A_1 e^{-400t} + A_2 e^{-1600t}$$

⑫

$$V_f = 0$$

$$V_o(0) = 0$$

$$i'(0) = 30 \text{ mA}$$

$$A_1 + A_2 = 0$$

$$\frac{i(0)}{C} = \frac{dV_o(0)}{dt} = 24000$$

$$-400A_1 + 1600A_2 = 24000$$

by

$$A_1 = 20 \quad A_2 = -20$$

$$V_o = 20 e^{-400t} - 20 e^{-1600t}$$

5

$$i_o = I_f + A_1' e^{-400t} + A_2' e^{-1600t}$$

$$I_f = 30 \text{ mA}$$

$$i_o(0) = 0$$

$$\frac{di_o}{dt}(0)$$

$$0 = 30 + A_1' + A_2'$$

$$-400A_1' = 1600A_2' = 0$$

$$A_1' = -40 \text{ mA}$$

$$A_2' = 10 \text{ mA}$$

$$i_o = 30 - 40 e^{-400t} + 10 e^{-1600t}$$

$$L \frac{di_o}{dt} \rightarrow V_o$$

check or another solve

The First Question

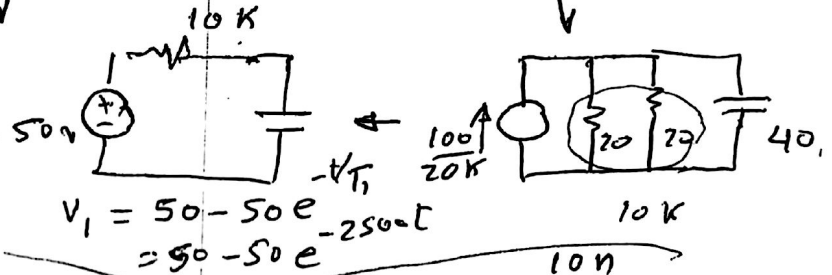
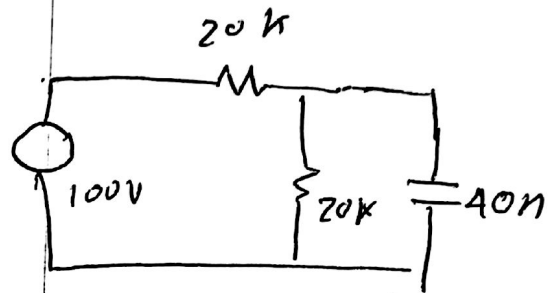
• $t = 0 \rightarrow 10 \text{ ms}$

$$T_1 = 10 \text{ K} + 40 \text{ n} = 400 \times 10^{-6}$$

$$5T_1 = 2000 \times 10^{-6} = 2 \text{ ms} < 10 \text{ ms}$$

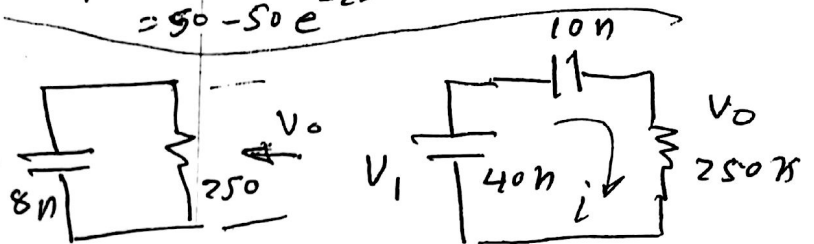
2 hence circuit approached steady state

1 $V_{C10} = 50 \text{ V}$



• $t > 10 \text{ ms}$

$$T_2 = 250 \text{ K} + 8 \text{ nF} = 2000 \times 10^{-6} \text{ s} = 2 \text{ ms}$$



$$V_0 = V_{C10} e^{-(t-0.01)/T_2} = 50 e^{-500(t-0.01)}$$

3 $V_0 = 50 e^{-500(t-0.01)} \quad t \geq 0$

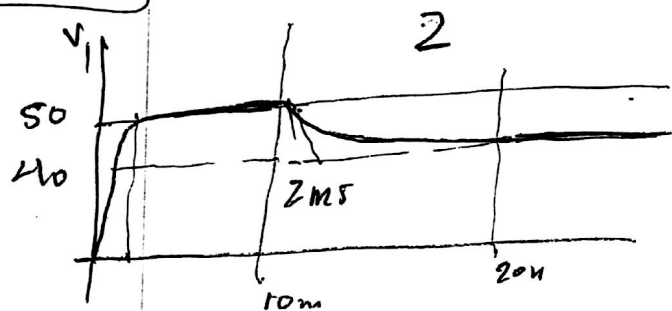
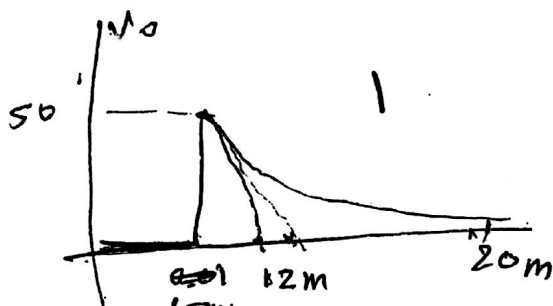
$$V_1 = \frac{1}{40 \text{ n}} \int i' dt + 50$$

$$i' = \frac{V_0}{250 \text{ K}} = \frac{200}{0.2} e^{-500(t-0.01)} \text{ mA}$$

$$V_1 = \frac{1}{40 \text{ n}} * 200 * 10^{-6} \int_0^t e^{-500(t-0.01)} dt + 50$$

$$= \frac{5 \times 10^3}{500} \left[e^{-500(t-0.01)} \right]_0^t + 50 = -10 e^{-500(t-0.01)} + 50$$

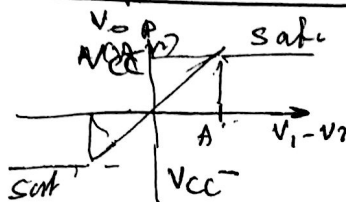
3 $V_1 = 10 e^{-500(t-0.01)} + 40$



The Fifth Question

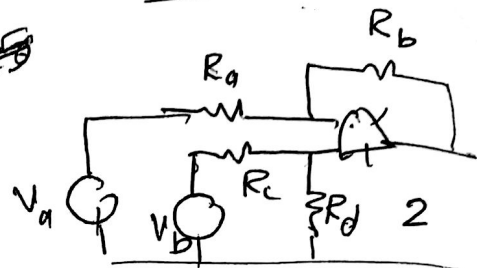
①

③



②

④



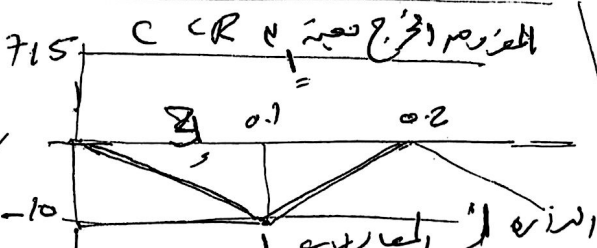
$$V_o = -\frac{R_f(R_a + R_b)}{R_a(R_f + R_b)} V_a - \frac{R_f}{R_b} V_b$$

For equal scaling for unity

$$\frac{R_b}{R_a} = \frac{R_f}{R_c} = 1$$

③

④



④

$$V_o = -\left[\frac{200}{100} V_a + \frac{200}{100} V_b + \frac{200}{40} V_c\right]$$

$V_a = 3$
 $V_b = 2$

④

$$V_o = -10 - 5 V_c$$

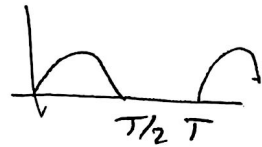
For $V_o = +12 \rightarrow V_c = -4.4 V$
 $V_o = -10 \rightarrow V_c = 0$

$$-4.4 < V_c < 0$$

⑤

$$a_0 = \frac{1}{T} \int_0^{T/2} V_m \sin \frac{2\pi}{T} t dt = \frac{V_m}{\pi}$$

$$= \frac{10}{\pi} = 3.183$$



⑤

$$a_k = \frac{2}{T} \int_0^{T/2} V_m \sin \frac{2\pi}{T} t \cos k\omega t dt$$

$$= \frac{V_m}{\pi} \left[\frac{1 + \cos k\pi}{1 - k^2} \right]$$

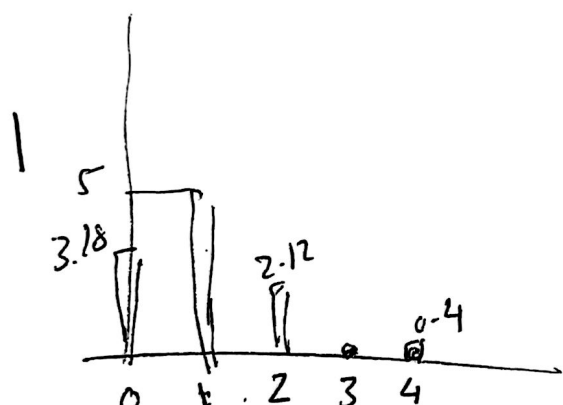
odd k: 0
even k: $\frac{2V_m}{\pi(1 - k^2)}$

$$b_k = \frac{2}{T} \int_0^{T/2} V_m \sin \frac{2\pi}{T} t \sin k\omega t dt$$

$$= 0 \quad k = 2, 3, 4$$

$$b_1 = \frac{V_m}{2}$$

n	0	1	2	3	4	5
C_n	$\frac{10}{\pi}$	$\frac{10}{2}$	$\frac{20}{3\pi}$	0	$\frac{20}{15\pi}$	0
	3.18	5	2.12	0	0.424	0



(2)

$$[b] \quad V_{BC} = 212 \angle 0^\circ$$

$$Z_1 = 20 \angle -60^\circ$$

$$Z_2 = 18 \angle 45^\circ$$

$$I_{BC1} = \frac{212 \angle 0^\circ}{20 \angle -60^\circ} = 10.6 \angle 60^\circ \text{ A}$$

$$I_{BC2} = \frac{212 \angle 0^\circ}{18 \angle 45^\circ} = 11.78 \angle -45^\circ \text{ A}$$

(i) for Load ①

$$P_1 = 212 \times 10.6 \cos 60^\circ = 1123.6 \text{ W}$$

$$Q_1 = 212 \times 10.6 \sin 60^\circ = 1946.13 \text{ VAR}$$

$$S_1 = 212 \times 10.6 = 2247.2 \text{ VA}$$

for Load ②

$$P_2 = 212 \times 11.78 \cos 45^\circ = 1765.9 \text{ W}$$

$$Q_2 = 212 \times 11.78 \sin 45^\circ = 1765.9 \text{ VAR}$$

$$S_2 = 212 \times 11.78 = 2497.36 \text{ VA}$$

(ii)

$$I_{bB} = \sqrt{3} \left[10.6 \angle 60-30^\circ + 11.78 \angle -45-30^\circ \right]$$

$$= \sqrt{3} \left[10.6 \angle 30^\circ + 11.78 \angle -75^\circ \right]$$

$$= \sqrt{3} \left[9.18 + j5.3 + 3.05 - j11.39 \right]$$

$$= \sqrt{3} \left[12.23 - j6.09 \right] = \sqrt{3} \times 13.66 \angle -26.47^\circ$$

$$I_{aA} = I_{bB} \angle 120^\circ = 23.66 \angle 93.53^\circ \text{ A}$$

$$I_{cC} = 23.66 \angle 213.53^\circ \text{ A}$$

$$(I_{BC} = 13.66 \angle 3.53^\circ) \text{ A}$$

(iii)

$$P_{\text{total}} = \sqrt{3} V_L I_L \cos \phi$$

$$= \sqrt{3} \times 212 \times 23.66 \times \cos(3.53^\circ)$$

$$= 8671.34 \text{ watt}$$

$$P_{\text{total}} = 3(P_1 + P_2) = 3(1123.6 + 1765.9)$$

$$= 8668.5 \text{ watt}$$

Q.4 (a)

$$(i) e_2 = M \frac{di_1}{dt} \quad , \quad M = 2k \sqrt{L_1 L_2} \\ = 50 \text{ mH} \\ = 0.05 \frac{d}{dt} (5 \sin 400t)$$

$$= 400 \times 5 \times 0.05 \cos 400t \\ = 100 \cos 400t \text{ V}$$

$$\lambda_{21} = M i_1 = 0.05 \times 5 \sin 400t \\ = 0.25 \sin 400t$$

$$\phi_{21} = \frac{\lambda_{21}}{N_2} = 0.25 \sin 400t \text{ mwb}$$

$$\phi_{11} = \frac{\phi_{21}}{k} = 0.5 \sin 400t \text{ mwb}$$

$$(iii) \mu_1 = \mu_2 = \frac{L_2}{(N_2)^2} = \frac{200 \times 10^{-3}}{(1000)^2} = 0.2 \times 10^{-6}$$

$$(ii) L_1 = (N_1)^2 \mu_1 \quad \rightarrow \quad N_1 = \sqrt{\frac{L_1}{\mu_1}} = 500 \text{ turns}$$

$$(b) M_{\max} = \sqrt{20 \times 25} = 22.36 \text{ mH} \quad (1')$$

$$(ii) v_s = 75 i_1 + 25 \times 10^{-3} \frac{d}{dt} (i_1 - i_2) + 22.36 \times 10^{-3} \frac{di_2}{dt}$$

$$0 = 20 \times 10^{-3} \frac{di_2}{dt} + 25 \times 10^{-3} \frac{d}{dt} (i_2 - i_1)$$

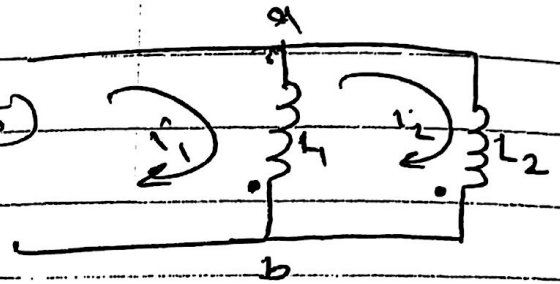
$$= \frac{22.36}{10^{-3}} \frac{d}{dt} (i_2 - i_1) = \frac{22.36}{10^{-3}} \frac{d}{dt} v_2$$

in frequency domain $\rightarrow v_s = 75 i_1 + j\omega \times 25 \times 10^{-3} (i_1 - i_2) + j\omega \times 22.36 \times 10^{-3} i_2$

$$0 = j\omega \times 20 \times 10^{-3} i_2 + j\omega \times 25 \times 10^{-3} (i_2 - i_1) \\ - j\omega \times 22.36 \times 10^{-3} (i_2 - i_1) - j\omega \times 22.36 \times 10^{-3} i_2$$

iii)

$$V_{ab} = L_1 \frac{d(i_1 - i_2)}{dt} + M \frac{di_2}{dt} \rightarrow (I)$$



$$0 = L_2 \frac{di_2}{dt} - M \frac{d(i_2 - i_1)}{dt} + L_1 \frac{d(i_2 - i_1)}{dt} - M \frac{di_2}{dt}$$

$$0 = (L_2 + L_1 - 2M) \frac{di_2}{dt} + (-L_1 + M) \frac{di_1}{dt}$$

$$\frac{di_2}{dt} = \frac{L_1 - M}{L_1 + L_2 - 2M} \frac{di_1}{dt} \rightarrow II$$

from II in I

$$V_{ab} = L_1 \frac{di_1}{dt} + (-L_1 + M) \frac{L_1 - M}{L_1 + L_2 - 2M} \frac{di_1}{dt}$$

$$= \frac{\cancel{L_1^2} + L_1 L_2 - 2M L_1 - \cancel{L_1^2} + M L_1 + M L_1 - M^2}{L_1 + L_2 - 2M} \frac{di_1}{dt}$$

$$= \frac{L_1 L_2 - M^2}{L_1 + L_2 - 2M} \frac{di_1}{dt}$$

$$\therefore L_{eq} = \frac{L_1 L_2 - M^2}{L_1 + L_2 - 2M} = \frac{20 \times 25 - (22.36)^2}{20 + 25 - 44.72}$$

= zero

(iv)

$$W_{\text{stored}} = \frac{1}{2} L_1 i_1^2 + \frac{1}{2} L_2 i_2^2 \pm M i_1 i_2$$

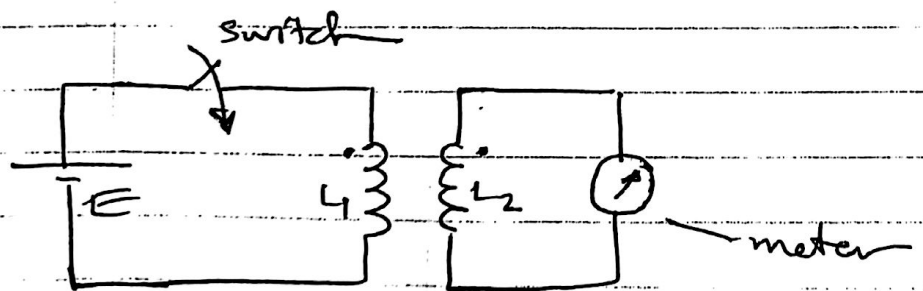
$$W > 0 \quad \rightarrow \quad \frac{1}{2} L_1 i_1^2 + \frac{1}{2} L_2 i_2^2 - M i_1 i_2 > 0$$

$$\underbrace{\left(\sqrt{\frac{L_1}{2}} i_1 - \sqrt{\frac{L_2}{2}} i_2 \right)^2}_{> 0} + \left(\sqrt{L_1 L_2} i_1 i_2 - M i_1 i_2 \right) > 0$$

$$\therefore \sqrt{L_1 L_2} i_1 i_2 - M i_1 i_2 > 0$$

$$M < \sqrt{L_1 L_2} \quad \rightarrow \quad \underline{M_{\text{max}} \sqrt{L_1 L_2}}$$

(c)



for (+ve) Reading of meter \rightarrow the dot location is right

for (-ve) Reading of meter \rightarrow one dot should be changed

(iv)

$$W_{\text{stored}} = \frac{1}{2} L_1 i_1^2 + \frac{1}{2} L_2 i_2^2 \pm M i_1 i_2$$

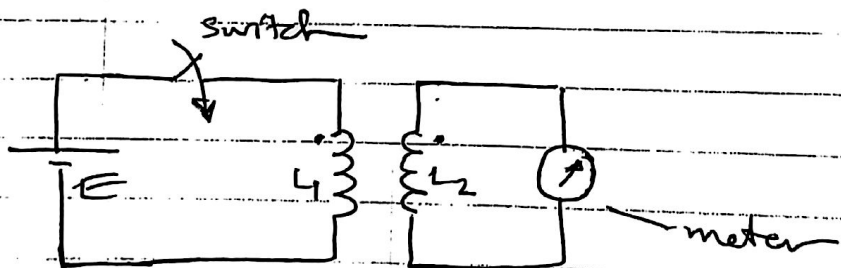
$$W > 0 \quad \rightarrow \quad \frac{1}{2} L_1 i_1^2 + \frac{1}{2} L_2 i_2^2 - M i_1 i_2 > 0$$

$$\underbrace{\left(\sqrt{\frac{L_1}{2}} i_1 - \sqrt{\frac{L_2}{2}} i_2 \right)^2}_{> 0} + \left(\sqrt{L_1 L_2} i_1 i_2 - M i_1 i_2 \right) > 0$$

$$\therefore \sqrt{L_1 L_2} i_1 i_2 - M i_1 i_2 > 0$$

$$M < \sqrt{L_1 L_2} \quad \rightarrow \quad \underline{M_{\text{max}} \sqrt{L_1 L_2}}$$

(c)



for (+ve) Reading of meter & the dot location is right

for (-ve) Reading of meter, one dot should be changed